



SHENTON
COLLEGE

Year 11 Mathematics Methods AEMAM Term 1 2020

Test 1 Counting and Probability

Calculator Free

Formula Sheet Allowed

Student Name: _____

Teacher: Alfonsi Feutrill Loh McRae White

Time Allowed: 25 minutes

Calculator Free:	/33
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Attempt **all** questions.

All necessary working and reasoning must be shown for **full marks**.

Marks may not be awarded for untidy or poorly arranged work.

Question 1.

[1, 1, 1, 1 = 4 marks]

Consider two sets $A = \{1, 2, 3, 5, 8, 13, 21\}$ and $B = \{1, 3, 6, 10, 15, 21\}$ and the universal set $U = \{x : x \in \mathbb{N}, 1 \leq x \leq 22\}$, where \mathbb{N} denotes the natural, or counting, numbers.

a) Use set notation to list the elements of the set:

(i) $A \cap B$

(ii) $A \cup B$

(iii) C , where $C = \{x : x \in A, x \text{ is even}\}$

b) State $n(\overline{A \cup B})$

Question 2.

[1, 2, 2, 2 = 7 marks]

Evaluate

a) $10! \div 7!$

b) $4! - 3! + 2! - 1! + 0!$

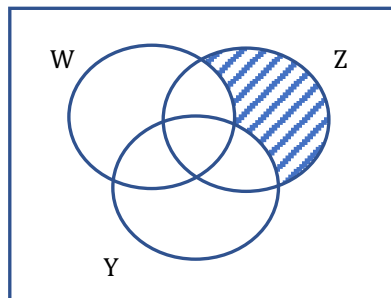
c) $\binom{8}{4}$

d) ${}^{100}C_{99} + {}^{50}C_{50}$

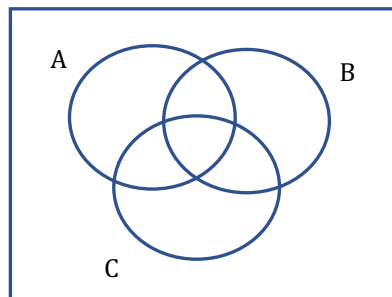
Question 3

[1, 1 = 2 marks]

a) Express the following shaded region using set notation



b) Shade $(B \cup \bar{C}) \cap A$



Question 4

[2, 3 = 5 marks]

Given $P(A) = 0.8 - x$, $P(A \cap B) = 0.1 + x$ and $P(B) = 0.4$,

a) if $P(\bar{A}) = 0.6$, determine the value x .

b) determine the value of x if the events A and B are independent.

Question 5

[4, 3 = 7 marks]

a) Use the two-way table and the information below to determine the value of $n(U)$.

$$n(A) = 32 \quad n(B) = 24 \quad n(\overline{A \cup B}) = 7 \quad n(U) = 8 \times n(A \cap B)$$

	B	\bar{B}	TOTAL
A			
\bar{A}			
TOTAL			

- b) Construct a Venn diagram showing three mutually exclusive events Q , R and S such that:
- events R and S are equally likely to occur;
 - the probability of event Q not occurring is 0.3; and,
 - $P(\overline{Q \cup R \cup S}) = 0.1$.

Question 6.

[2, 2, 3, 1 = 8 marks]

- a) Expand $(a + b)^4$.
- b) Using the properties of Pascal's triangle, determine the sum of the coefficients of $(a + b)^2 + (a + b)^3 + (a + b)^4$.
- c) Without showing the expansion, identify the coefficient of p^3 in the expansion of $(1 - 3p)^5$.
- d) Briefly explain why the sum of the coefficients in $(1 - 3p)^5$ will not equal 2^5 , as implied by the fifth row of Pascal's triangle.

End of Calculator-Free Section

Question 9.**[2, 1, 1, 2 = 6 marks]**

A corner deli recorded its lunchtime sales for a week. During this time, it served a total of 621 customers. 233 customers bought a burger and a cup of hot chips. An additional 189 customers bought just a cup of hot chips. 94 customers bought items other than burgers or chips.

a) Complete the two-way table below.

	B	\bar{B}	TOTAL
C	233		
\bar{C}		94	
TOTAL			621

b) Determine the probability (to 4 decimal places):

(i) that a customer bought a burger;

(ii) that a customer bought a burger, given that they bought chips;

c) Hence, comment on whether there is sufficient evidence to indicate that a customer buying a burger is independent of the customer buying chips.

Question 10.

[6 marks]

A committee of five current Year 11 students is to be established to plan next year's Year 12 ball. Seven boys and eight girls put their names forward to be on the committee.

Given that the committee must have at least one boy, determine the probability that it has more boys than girls.

End of Calculator Assumed Section